

# PyCirc - Python Logic Circuit Modeling and Simulation Package

- [Link to GITHUB repository](#)
- [Link to the Google Colaboratory notebook](#)
  - The Google Colaboratory notebook has the advantage that you can run PyCirc from it without having to install PyCirc or even Python on your local system.
  - You first need to copy it to your google drive (or github repository)
  - You can also download it to your local device and open it as a Jupyter notebook (if you have it installed with your Python).

## ▼ Installing the PyCirc package

- The **PyCirc** package can be installed on your local system by running the following command from the command line

```
pip install pycirc
```

- Or you may try running one of the following commands from this notebook.
- If you are running it from a Jupyter notebook on your local system, then it will be installed on your device.

```
# To install from this notebook, uncomment the next line and run this cell.  
# %pip install pycirc  
# This should also work:  
# !pip install --upgrade pycirc  
  
# After installation, you have to restart this notebook.  
# Make sure to comment the %pip or !pip lines above to avoid reinstall each time  
  
# To uninstall the package use:  
# %pip uninstall pycirc  
# or  
# !pip uninstall pycirc
```

- **After installation, you may need to restart this notebook.**

## ▼ Loading the PyCirc package

- After installing the **PyCirc** package, you need to import it.
- The following command imports **PyCirc** to your Python interpreter.

```
from pycirc import *  
  
Loading builtin box cells..
```

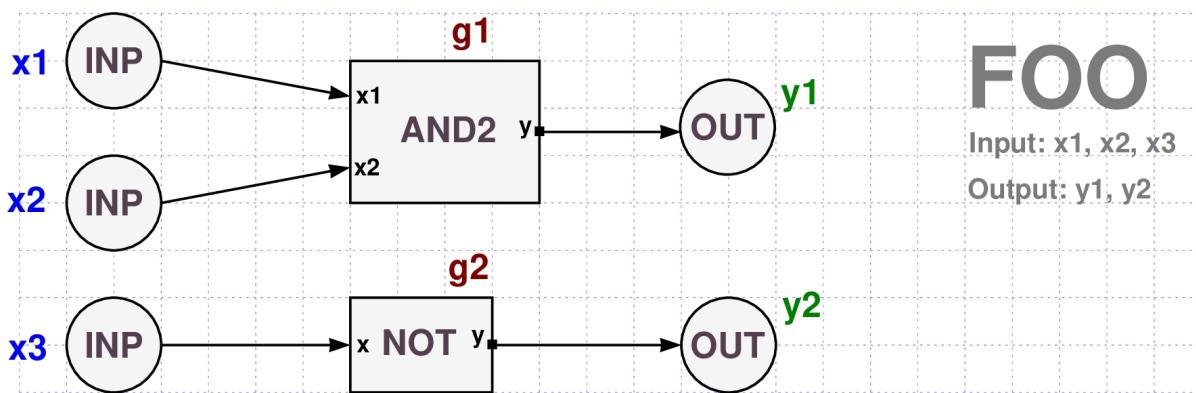
## Introduction

- **PyCirc** is a new Python package for modeling and simulating simple Logic Circuits specifically designed for educational use in introductory computation and digital logic college course.
- As such, it was primarily tuned for simplicity, readability convenience, and fast learning curve.
  - Less for speed or industrial production.
- It is a light weight package especially designed for small to medium scale circuits, such as those that are studied in introductory academic courses on the theory of computation and electronic digital design.
- Its main characteristic is that a digital circuit can be easily defined by a series of simple Python commands, rather than an external static language.
- So, the only requirement is a basic knowledge of the Python programming language, with a little programming skill.
- Experienced Python programmers can probably benefit a lot more from this package.
- It can be a useful companion for theoretical courses on computation models and languages who wish also to engage the students with some programming experience and skills.
  - It is planned to be used in such a course by the author (Hebrew book at <http://samyzaf.com/afl.pdf>).
  - It enables students to easily model and experiment with
    - Typical logic circuit design
    - Logic Circuit Modeling and Validation
    - Logic Circuit Testing
    - Logic problem solving
- It does provide an opportunity for students to develop and practice some programming skills while covering the theoretical computation course.
- In this tutorial, we will cover:

1. Basic usage of PyCirc for modeling and manipulating Logic Circuits.
2. A short survey of the commands and tools of the **PyCirc** package.
3. Examples for modeling Logic Circuits and their manipulation.
4. Advanced usage of PyCirc for experienced Python programmers (TODO).

## ▼ Example 1: The Circuit FOO

- We start with a very simple logic circuit which we call "**FOO**"
- Inputs gates:  $x_1, x_2, x_3$
- Output gates:  $y_1, y_2$
- Logic action:  $(y_1, y_2) = (x_1 \wedge x_2, \neg x_3)$
- This circuit can be represented by the following **PyCirc Diagram**



- A **PyCirc diagram** is a simplified form of circuit diagram in which gates are represented by text blocks rather than special shape symbols.
  - Many students find the usual gate symbols intimidating and hard to memorize.
  - Plain text on a circle or a rectangle seems to be more convenient, especially for computation theory courses in which most of the participants do not have any electronics background (or plan to go in this direction).
- **Input and output gates** are represented by circles with an **INP/OUT** labels.
- The other **logic gates** are represented by rectangular blocks with input/output **pins** near the block edges.
  - Input gate names are **blue colored**.
  - Output gate names are **green colored**.
  - Logic gate names are **brown colored**.
- **Connections ("Wires")** are represented by arrowed lines from source pin to target pin.
- A **pin** is either an input/output gate or a named entry/exit point to a logic gate.

- In the above diagram we have 5 wires and 10 pins:
  - 3 Input gates:  $x_1, x_2, x_3$
  - 2 output gates:  $y_1, y_2$
  - 5 Block pins:  $g_1/x_1, g_1/x_2, g_1/y, g_2/x, g_2/y$
- Note the special notation **g/p** for the block pins.
  - **g** stands for the gate name and **p** is the input/output name of the cell type of the gate.
- Here is the **PyCirc code** for modeling this circuit:

```
Define("foo")
GATE (name="x1", type="inp")
GATE (name="x2", type="inp")
GATE (name="x3", type="inp")
GATE (name="y1", type="out")
GATE (name="y2", type="out")
GATE (name="g1", type="and2")
GATE (name="g2", type="not")

WIRE ("x1", "g1/x1")
WIRE ("x2", "g1/x2")
WIRE ("x3", "g2/x")
WIRE ("g1/y", "y1")
WIRE ("g2/y", "y2")
EndDef()

Cell = foo: Validity check: OK.
<pycirc.pycirc.PyCirc at 0x7f011d8fae90>
```

- Notice that this is a **pure Python code!**
  - So you need to **run** its cell in order to execute it.
- A circuit definition starts with the `Define()` function call which accepts the circuit name as its first argument.
- The definition ends with the `EndDef()` function call.
- A circuit definition consists of `GATE` and `WIRE` commands.
  - The `GATE` function accepts the name and the logic type of the gate.
  - The `WIRE` function connects a source pin to a target pin.
- A pin notation `g/p` consists of a gate name `g` and a pin name `p`.
  - The pin `p` is either an input or an output pin of the gate.
- For example the expression `"g1/x2"` designates the input pin `"x2"` of the gate `"g1"`.

- The flag "name=" is optional. It is enough to specify the name only:

```
GATE("x1", type="inp")
```

- The 'type' flag indicates the logic cell name to which the gate is an instance of.
- **Input gates** are the circuit elements in which we feed the input (boolean values).
- **Output gate** are the circuit elements from which we read the output after its computation is done.
- All remaining gates are called **logical gates**.
- They usually have incoming wires and outgoing wires and they perform some logic action.
- We repeat: the above definition of the cell **FOO** is also a **pure Python code!**
- This means that you can include it inside longer Python programs/scripts and manipulate cells dynamically.
  - For example, it is possible to add or remove gates or wires in a circuit dynamically and run it for optimization goals.

## ▼ Circuit libraries

- After successful design of a circuit such as **FOO**, it can be placed as a single file 'foo.py' in a **circuit library** and loaded by the **load** command

```
load("foo")
```

- A **circuit library** is simply a directory that contains circuit files.
- You may have several directories, including directories residing on far Internet locations.
- You specify the library with a list such as

```
set_path(["c:/eda/pycirc/lib", "d:/cmfl/code/logcirc/lib", "https://samyzaf.com/pyc
```



- We will use this library path in this notebook, but you can download all circuit files from the following url, place them on your local computer, and change the path accordingly.
- In most cases it is better to use the **need** command

```
need("foo")
```

which loads a circuit only if it was not already loaded.

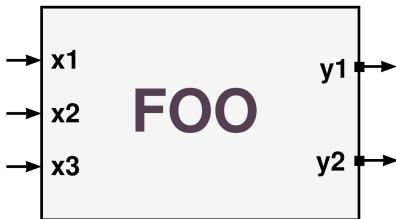
```
# You need to edit this list.  
# Replace the first two library paths to ones in your local system.  
# Or just leave the last one to load cells from pycirc web site.  
  
set_path(["c:/eda/pycirc/lib", "d:/cmfl/code/logcirc/lib1", "https://samyzaf.com/pycirc/cells"])
```

- You may want to copy the circuit library that we use in this notebook to your local pc.
- Here is a link to a zip file that contains all the cells we use here:
  - [Click to download lib.zip](#)
- You can also browse this library and pick individual files from it
  - [Click to browse the library](#)
- After copying it to your local space, you can add more cells to it, or create more libraries like it.
- If you do, don't forget to update the new list with the **set\_path** command:

```
set_path([ dir1, dir2, url1, url2, ...])
```

## Gates as Cell Instances

- The term **cell** means a packaged circuit or any other function which accepts inputs and provide output. After defining a circuit for example, it is "packaged" as a cell which hides its content and only exposes its input and output.
- Once we have defined a cell such as **FOO**, we can use it as a building block element inside the definitions of new cells.
- Every logic gate in a logic circuit must be an instance of some cell.
- Typically, there can be several instances of the same cell in a logic circuit definition.
- This is how the **FOO** cell is represented as a single block element in a logic circuit
- It appears as a named black box with only entry and exit points (pins)



## ▼ The Circuit FRED

- Here is an example of cell called **FRED** which uses an instance of the cell **FOO** as one of its building blocks.

```
# CELL: FRED
# This cell is using a gate of type FOO which we defined earlier
# It will be automatically loaded.

Define("fred")

GATE("x1", type="inp")           # No need to use: name="x1"
GATE("x2", type="inp")
GATE("y1", type="out")
GATE("y2", type="out")
GATE("g1", type="foo")           # Here we define a gate g1 of type FOO !     <<<<
GATE("g0", type="zero")

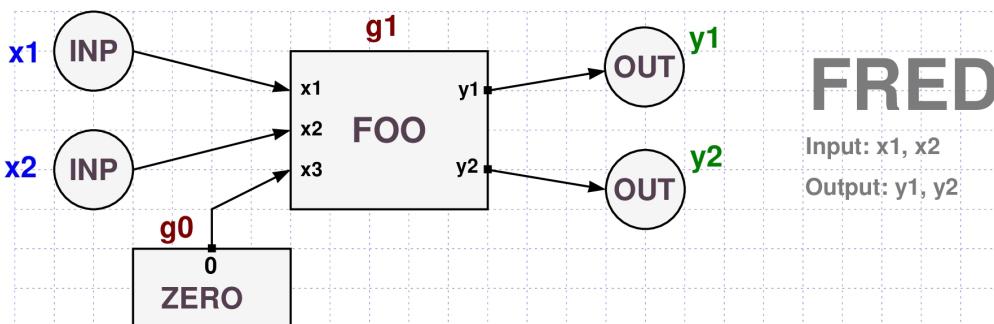
WIRE("x1", "g1/x1")
WIRE("x2", "g1/x2")
WIRE("g0", "g1/x3")
WIRE("g1/y1", "y1")
WIRE("g1/y2", "y2")

EndDef()

Cell = fred: Validity check: OK.
<pycirc.pycirc.PyCirc at 0x7f0121ff1e50>
```

- This is the standard for defining a new circuit from a regular Python code.
  - Within a library tree, the Define/EndDef lines must be omitted since the name of the circuit, beginning and end, are easily inferred from the circuit file.
- Usually every circuit is defined in a single file "**name.py**", and kept within a library directory, but several circuit definitions can also reside in a single file and imported to a Python code via the Python import mechanism.

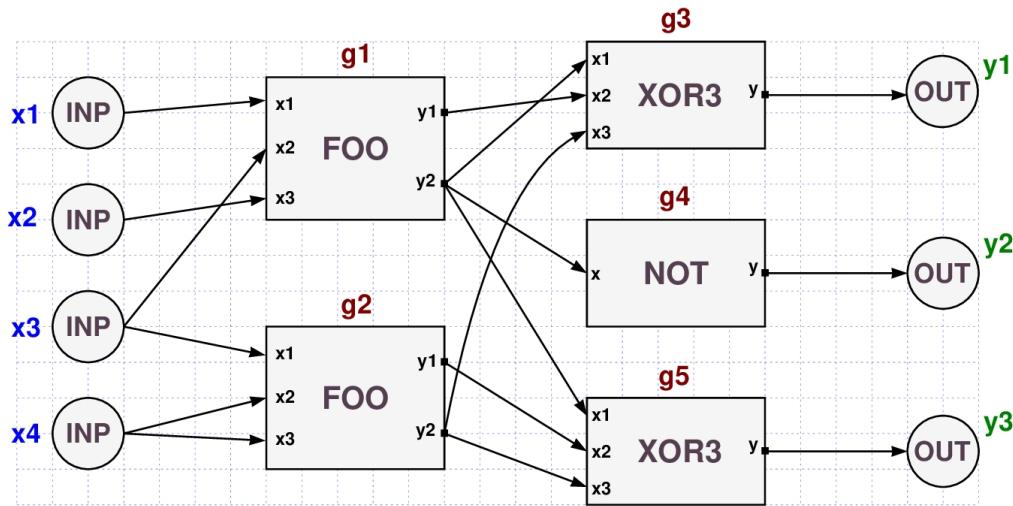
- You create a library by
  - allocating a folder or a url for it.
  - putting all your circuit definitions in this folder (one circuit per file).
  - adding this directory (or url) to the **set\_path** list (see above).
  - Note that the Define/EndDef lines are omitted in a circuit file!
- Note the line `GATE("g1", type="foo")` in which the gate of type **FOO** is declared! It automatically triggers the loading of **FOO** (if it wasn't already loaded).
- It is easy to draw a **PyCirc Diagram** from the above definition



- Note that we used the **ZERO** cell which has no inputs, and only one constant 0 output.
- It is the hardware equivalent of a **boolean constant**.
  - We use it to fix the input x3 of gate g1 to zero.
- The **ZERO** cell is a fundamental **PyCirc** cell which is automatically loaded when PyCirc starts.

## ▼ The Circuit HAM

- The following cell **HAM** contains two gates of type **FOO** and two gates of type **XOR3**.
- The **XOR3** cell is a typical **xor** cell with 3 input gates (built in PyCirc).
- It also contains one gate of type **NOT**.
- The **XOR3** and **NOT** cells are built in types of **PyCirc** and are loaded automatically when **PyCirc** starts.



# HAM

Input: x1, x2, x3, x4  
Output: y1, y2, y3

- Here is a **PyCirc code** for modeling this cell.
- Note the **compressed notation** style for writing shorter code.

```

# CELL: HAM
# This cell is using the FOO cell which we defined earlier
# "xor3" is a basic cell in PyCirc - it is built in and loaded at start time.

Define("ham")

GATE("x<1:4>", type="inp")          # Input gates: x1, x2, x3, x4
GATE("y<1:3>", type="out")           # Output gates: y1, y2, y3
GATE("g1; g2", type="foo")             # Here we define two gates g1 and g2 of 1
GATE("g4", type="not")                # Here we define two gates g3 and g5 of 1
GATE("g3; g5", type="xor3")           # Input gates: x1, x2, x3, x4

WIRE("x1", "g1/x1")
WIRE("x2", "g1/x3")
WIRE("x3", "g1/x2; g2/x1")           # Two wires defined in one line: "x3" ->
WIRE("x4", "g2/x2; g2/x3")
WIRE("g1/y1", "g3/x2")
WIRE("g1/y2", "g3/x1; g4/x; g5/x1") # Three wires defined in one line!
WIRE("g2/y1", "g5/x2")
WIRE("g2/y2", "g3/x3; g5/x3")
WIRE("g3/y", "y1")
WIRE("g4/y", "y2")
WIRE("g5/y", "y3")

EndDef()

Cell = ham: Validity check: OK.
<pycirc.pycirc.PyCirc at 0x7f011d91b6d0>
  
```

- Note that "x<1:4>" stands for x1, x2, x3, x4
- Instead of writing 4 lines of code

```
GATE("x1", type="inp")
GATE("x2", type="inp")
GATE("x3", type="inp")
GATE("x4", type="inp")
```

We can write one equivalent line!

```
GATE("x<1:4>", type="inp")
```

- Instead of writing

```
WIRE("g1/y2", "g3/x1")
WIRE("g1/y2", "g4/x")
WIRE("g1/y2", "g5/x1")
```

We can simply write

```
WIRE("g1/y2", "g3/x1; g4/x; g5/x1")
```

- Arguments can also be lists or tuples of compressed names!

```
WIRE("g1/y2", ["g%s/x%s" % (i,) for i in range(20)])
```

- More on **compressed notation** in the examples below.
- The only supported modes:

- one to one
- one to many
- many to one
- n to n

## ▼ Cell Query and Manipulation

- After defining the cell **HAM** we may start performing all kind of queries on it.

- First we need to get a reference to it.

```
# Get a reference to HAM
```

```
ham = PyCirc["ham"]
```

- This gives us a PyCirc reference to our `ham` circuit object, which we can use to manipulate the cell.
- `PyCirc` is the name of the Python class which creates logic circuit objects.
- The class `PyCirc` keeps a map between the name and the reference of every logic circuit created by it.
- So if you have the name of an existing logic circuit, you can get a handle for it by using

```
ref = PyCirc[name]
```

anywhere in your code.

- You may use `ref` as any other Python object handle for querying and manipulating the cell object.

```
# Print the gates in the circuit HAM
```

```
for g in ham.gates:
    print(g)
```

```
gate id=13: name=x1, type=inp, value=(None), depth=0
gate id=14: name=x2, type=inp, value=(None), depth=0
gate id=15: name=x3, type=inp, value=(None), depth=0
gate id=16: name=x4, type=inp, value=(None), depth=0
gate id=17: name=y1, type=out, value=(None), depth=3
gate id=18: name=y2, type=out, value=(None), depth=3
gate id=19: name=y3, type=out, value=(None), depth=3
gate id=20: name=g1, type=foo, value=(y1=None, y2=None), depth=1
gate id=21: name=g2, type=foo, value=(y1=None, y2=None), depth=1
gate id=22: name=g4, type=not, value=(y=None), depth=2
gate id=23: name=g3, type=xor3, value=(y=None), depth=2
gate id=24: name=g5, type=xor3, value=(y=None), depth=2
```

```
# Count the number of gates in the circuit HAM
```

```
print(len(ham.gates))
```

```
# Get names of input gates

for x in ham.input:
    print(x.name)

x1
x2
x3
x4

# Get names of output gates

for x in ham.output:
    print(x.name)

y1
y2
y3

# Count the number of wires in the circuit HAM
print(len(ham.wires))

16

# List all XOR3 gates

for g in ham.gates:
    if g.type == "xor3":
        print(g)

gate id=23: name=g3, type=xor3, value=(y=None), depth=2
gate id=24: name=g5, type=xor3, value=(y=None), depth=2

# Get a reference to gate "g1"
g1 = ham["g1"]

# Print all outcoming gates from g1
for g in ham.out_gates(g1):
    print(g)

gate id=22: name=g4, type=not, value=(y=None), depth=2
gate id=23: name=g3, type=xor3, value=(y=None), depth=2
gate id=24: name=g5, type=xor3, value=(y=None), depth=2
```

- This gives us only gates and ignores pins.
- To get pin connections we need to dig a bit deeper.

```
# Print all outgoing wires from g1
for w in ham.out_wires(g1):
    print(w)

    wire id=16:
        source=gate id=20: name=g1, type=foo, value=(y1=None, y2=None), depth=1
        target=gate id=23: name=g3, type=xor3, value=(y=None), depth=2
        source=y1
        target=x2
    wire id=17:
        source=gate id=20: name=g1, type=foo, value=(y1=None, y2=None), depth=1
        target=gate id=23: name=g3, type=xor3, value=(y=None), depth=2
        source=y2
        target=x1
    wire id=18:
        source=gate id=20: name=g1, type=foo, value=(y1=None, y2=None), depth=1
        target=gate id=22: name=g4, type=not, value=(y=None), depth=2
        source=y2
        target=x
    wire id=19:
        source=gate id=20: name=g1, type=foo, value=(y1=None, y2=None), depth=1
        target=gate id=24: name=g5, type=xor3, value=(y=None), depth=2
        source=y2
        target=x1
```

- This is too verbose.
- We want to get a cleaner list of pin connections:

```
for w in ham.out_wires(g1):
    print("%s => %s" % (w.source, w.target))

g1/y1 => g3/x2
g1/y2 => g3/x1
g1/y2 => g4/x
g1/y2 => g5/x1

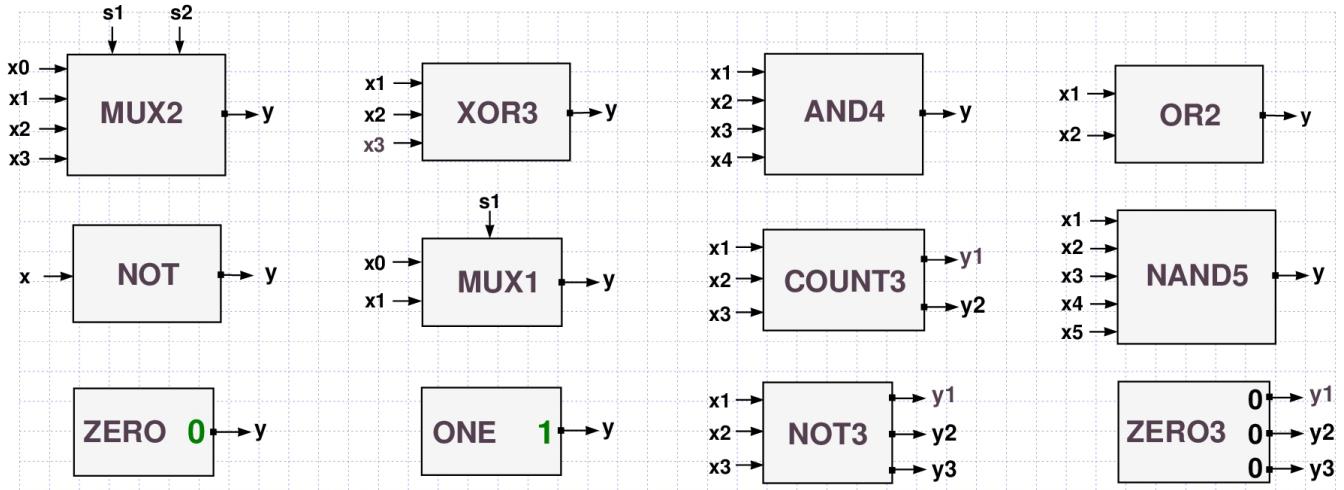
# Get a reference to gate "g3"
g3 = ham["g3"]

# Print all incoming wires to gate g3
for w in ham.in_wires(g3):
    print("%s ==> %s" % (w.source, w.target))

g1/y1 ==> g3/x2
g1/y2 ==> g3/x1
g2/y2 ==> g3/x3
```

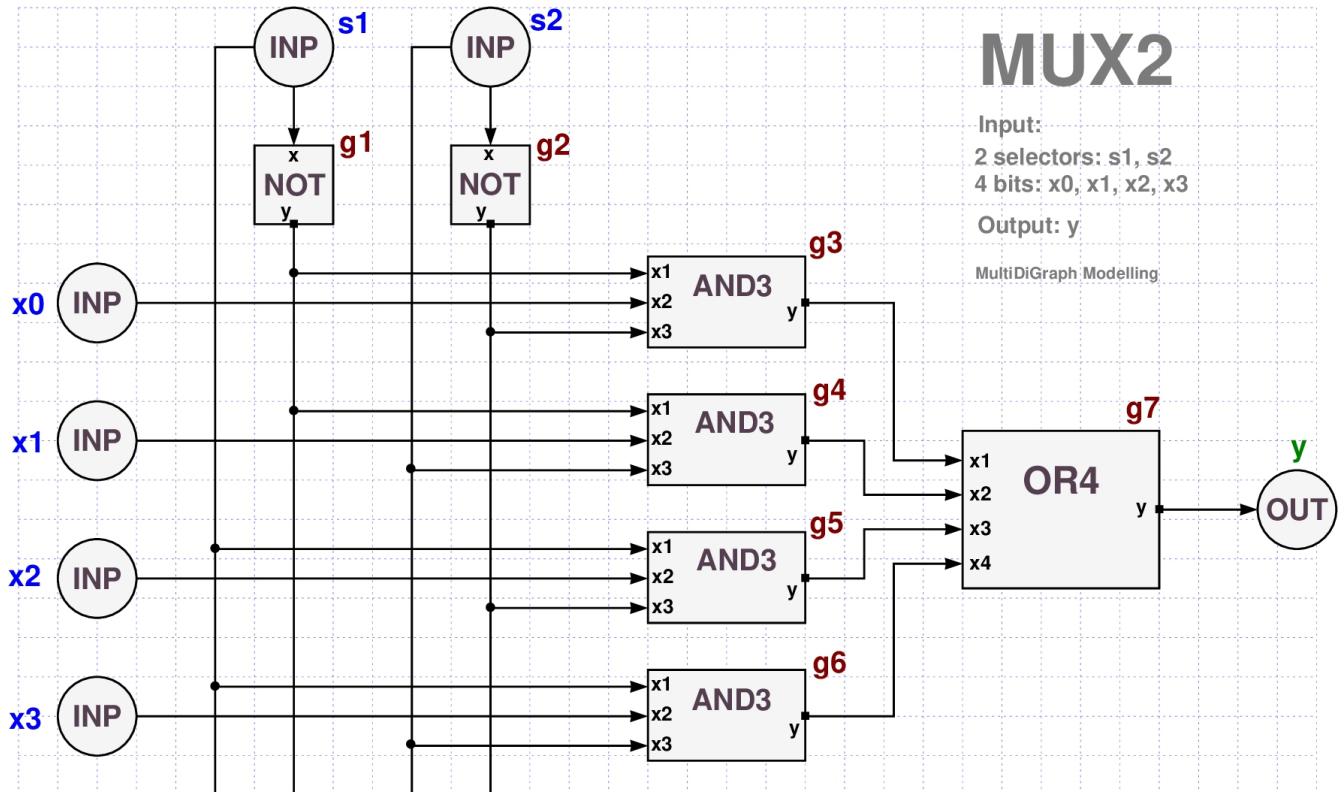
- Note the `ham["g3"]` expression in the first line.

- The PyCirc object `ham` has been overloaded as a dictionary which maps gate and wire names to their reference.
- The following diagram displays examples of typical circuit representations in the PyCirc package.



## ▼ 4x1 Multiplexer Design

- Multiplxers are important circuit elements in electronic design.
- Here is a simple PyCirc Design Diagram and code for a 4x1 Multiplexer circuit (aka MUX2)



```
# File for MUX2
# input: x3, x2, x1, x0, s2, s1
```

```
# output: y

GATE("x0", type="inp")
GATE("x1", type="inp")
GATE("x2", type="inp")
GATE("x3", type="inp")
GATE("s1", type="inp")
GATE("s2", type="inp")
GATE("y", type="out")
GATE("g1", type="not")
GATE("g2", type="not")
GATE("g3", type="and3")
GATE("g4", type="and3")
GATE("g5", type="and3")
GATE("g6", type="and3")
GATE("g7", type="or4")

WIRE("s1", "g1/x")
WIRE("s1", "g5/x1")
WIRE("s1", "g6/x1")
WIRE("s2", "g2/x")
WIRE("s2", "g4/x3")
WIRE("s2", "g6/x3")
WIRE("x0", "g3/x2")
WIRE("x1", "g4/x2")
WIRE("x2", "g5/x2")
WIRE("x3", "g6/x2")
WIRE("g1/y", "g3/x1")
WIRE("g1/y", "g4/x1")
WIRE("g2/y", "g3/x3")
WIRE("g2/y", "g5/x3")
WIRE("g3/y", "g7/x1")
WIRE("g4/y", "g7/x2")
WIRE("g5/y", "g7/x3")
WIRE("g6/y", "g7/x4")
WIRE("g7/y", "y")
```

Cell = mux2: Validity check: OK.  
 <pycirc.pycirc.PyCirc at 0x7f011d8eff10>



\* This is long. Took 35 lines of code to  
 \* With \*\*compressed notation\*\* it takes  
 \* In addition, \*\*compressed notation\*\* c  
 buttons the circuit structure as it is

- This is long. Took 35 lines of code to define this circuit.

\* Remember that this is a clean Python code, so you can use Python comments, and other Python commands.

- With **compressed notation** it takes only 15 lines!
- In addition, **compressed notation** can help us understand better the circuit structure, as it is displayed in one paragraph.
- Remember that this is a clean Python code, so you can use Python comments, and other Python commands.

```
# File: mux2.py
# MUX2 (4x1 Multiplexer)
# input: x3, x2, x1, x0, s2, s1
# output: y

GATE("x<0:3>", type="inp")           # 4 bits
GATE("s1;s2", type="inp")              # 2 selectors
GATE("y", type="out")
GATE("g1; g2", type="not")
GATE("g<3:6>", type="and3")          # 4 gates of basic type "and3"
GATE("g7", type="or4")

WIRE("s1", "g1/x; g5/x1; g6/x1")
WIRE("s2", "g2/x; g4/x3; g6/x3")      # 3 wires!
WIRE("x<0:3>", "g<3:6>/x2")
WIRE("g1/y", "g3/x1; g4/x1")
WIRE("g2/y", "g3/x3; g5/x3")
WIRE("g<3:6>/y", "g7/x<1:4>")       # 4 wires
WIRE("g7/y", "y")

Cell = mux2: Validity check: OK.
<pycirc.pycirc.PyCirc at 0x7f0124aa3e90>
```

```
# get a grip on our MUX2 object
```

```
mux2 = PyCirc["mux2"]
```

- Lets print the list of gates in our circuit mux2:

```
for g in mux2.gates:
    print(g)

    gate id=39: name=x0, type=inp, value=(None), depth=0
```

```
gate id=40: name=x1, type=inp, value=(None), depth=0
gate id=41: name=x2, type=inp, value=(None), depth=0
gate id=42: name=x3, type=inp, value=(None), depth=0
gate id=43: name=s1, type=inp, value=(None), depth=0
gate id=44: name=s2, type=inp, value=(None), depth=0
gate id=45: name=y, type=out, value=(None), depth=4
gate id=46: name=g1, type=not, value=(y=None), depth=1
gate id=47: name=g2, type=not, value=(y=None), depth=1
gate id=48: name=g3, type=and3, value=(y=None), depth=2
gate id=49: name=g4, type=and3, value=(y=None), depth=2
gate id=50: name=g5, type=and3, value=(y=None), depth=2
gate id=51: name=g6, type=and3, value=(y=None), depth=1
gate id=52: name=g7, type=or4, value=(y=None), depth=3
```

- This is too verbose, but useful for debugging purposes.
- To get more specific info, you may use code like this:

```
print("Gates list")
for g in mux2.gates:
    print("name = %s,      type = %s" % (g.name, g.type))

Gates list
name = x0,      type = inp
name = x1,      type = inp
name = x2,      type = inp
name = x3,      type = inp
name = s1,      type = inp
name = s2,      type = inp
name = y,       type = out
name = g1,      type = not
name = g2,      type = not
name = g3,      type = and3
name = g4,      type = and3
name = g5,      type = and3
name = g6,      type = and3
name = g7,      type = or4
```

## ▼ Truth Assignments in PyCirc

- Truth assignment for a boolean formula or a boolean circuit is a mapping between its boolean variables and the two boolean values  $\{0, 1\}$ .
- In PyCirc, trurth assignment is modeled by a Python class called **Assign**, which is a subclass of the standard Python dictionary class **dict**.
- An **Assign** object maps a list of gate names to one of three values:  $\{0, 1, \text{None}\}$ .
- The value `None` indicates uninitialized state.
- Here is a simple example for defining an assignment on four input variables.

```
a = Assign(["x1", "x2", "x3", "x4"], [0,0,1,1])
```

Here are some code examples for manipulating an Assign object

```
print(a)
```

```
x1=0, x2=0, x3=1, x4=1
```

```
for x in a.names:  
    print(x)
```

```
x1  
x2  
x3  
x4
```

```
a.bits()
```

```
'0011'
```

```
a.bits("x<1:3>")
```

```
'001'
```

```
a.bits(["x2", "x4"])
```

```
'01'
```

- An assignment object `a` is callable (i.e., can be called as a function)
- The result of the call `a()` is the list of its bit values.

```
a()
```

```
[0, 0, 1, 1]
```

- You can pass bit names in expanded or compressed form:

```
a(["x2", "x3"])
```

```
[0, 1]
```

```
a("x<2:4>")
```

```
[0, 1, 1]
```

- It is also possible to create an **Assign** object from keyword/value pairs, just like in a Python dictionary.

```
a = Assign.fromKeys(x1=0, x2=0, x3=1, x4=1)
print(a)
```

```
x1=0, x2=0, x3=1, x4=1
```

- The **Assign** class also accepts names in compressed form.
- The default of the second argument is `None` for all bits.

```
a = Assign("x<1:4>")
print(a)
```

```
x1=None, x2=None, x3=None, x4=None
```

- The `None` value indicates that the input is uninitialized.
- Use the following to initialize all values to zero (or one).

```
a = Assign("x<1:4>", 0)
print(a)
```

```
x1=0, x2=0, x3=0, x4=0
```

- The **Assign** class also has a static method **Assign.iter** for creating an iterator for looping over all truth assignments!

```
gates = ['x1', 'x2', 's1', 's2']
for a in Assign.iter(gates):
    print(a)
```

```
x1=0, x2=0, s1=0, s2=0
x1=0, x2=0, s1=0, s2=1
x1=0, x2=0, s1=1, s2=0
x1=0, x2=0, s1=1, s2=1
x1=0, x2=1, s1=0, s2=0
x1=0, x2=1, s1=0, s2=1
x1=0, x2=1, s1=1, s2=0
x1=0, x2=1, s1=1, s2=1
x1=1, x2=0, s1=0, s2=0
x1=1, x2=0, s1=0, s2=1
```

```
x1=1, x2=0, s1=1, s2=0
x1=1, x2=0, s1=1, s2=1
x1=1, x2=1, s1=0, s2=0
x1=1, x2=1, s1=0, s2=1
x1=1, x2=1, s1=1, s2=0
x1=1, x2=1, s1=1, s2=1
```

```
gates = ['x1', 'x2', 's1', 's2']
for a in Assign.iter(gates):
    print(a.bits())
```

```
0000
0001
0010
0011
0100
0101
0110
0111
1000
1001
1010
1011
1100
1101
1110
1111
```

```
gates = ['x1', 'x2', 's1', 's2']
for a in Assign.iter(gates):
    bitlist = a()
    print(bitlist)
```

```
[0, 0, 0, 0]
[0, 0, 0, 1]
[0, 0, 1, 0]
[0, 0, 1, 1]
[0, 1, 0, 0]
[0, 1, 0, 1]
[0, 1, 1, 0]
[0, 1, 1, 1]
[1, 0, 0, 0]
[1, 0, 0, 1]
[1, 0, 1, 0]
[1, 0, 1, 1]
[1, 1, 0, 0]
[1, 1, 0, 1]
[1, 1, 1, 0]
[1, 1, 1, 1]
```

## ▼ How to initialize a PyCirc object?

- When you create a new Pycirc circuit, none of the input gates are initialized.
- All gate values equal `None`.

```
for g in mux2.gates:
    print(g)

    gate id=39: name=x0, type=inp, value=(None), depth=0
    gate id=40: name=x1, type=inp, value=(None), depth=0
    gate id=41: name=x2, type=inp, value=(None), depth=0
    gate id=42: name=x3, type=inp, value=(None), depth=0
    gate id=43: name=s1, type=inp, value=(None), depth=0
    gate id=44: name=s2, type=inp, value=(None), depth=0
    gate id=45: name=y, type=out, value=(None), depth=4
    gate id=46: name=g1, type=not, value=(y=None), depth=1
    gate id=47: name=g2, type=not, value=(y=None), depth=1
    gate id=48: name=g3, type=and3, value=(y=None), depth=2
    gate id=49: name=g4, type=and3, value=(y=None), depth=2
    gate id=50: name=g5, type=and3, value=(y=None), depth=2
    gate id=51: name=g6, type=and3, value=(y=None), depth=1
    gate id=52: name=g7, type=or4, value=(y=None), depth=3
```

- In order to run a circuit, we first need to initialize its input gates.
- Lets assign values to mux2 input gates, and check again the values of its gates.
- The **PyCirc set** method is used

```
a = Assign.fromKeys(x3=1, x2=0, x1=1, x0=0, s2=0, s1=1)
mux2.set(a)      # Initializing the cel MUX2 with assignment a
```

```
for g in mux2.gates:
    print(g)

    gate id=39: name=x0, type=inp, value=(0), depth=0
    gate id=40: name=x1, type=inp, value=(1), depth=0
    gate id=41: name=x2, type=inp, value=(0), depth=0
    gate id=42: name=x3, type=inp, value=(1), depth=0
    gate id=43: name=s1, type=inp, value=(1), depth=0
    gate id=44: name=s2, type=inp, value=(0), depth=0
    gate id=45: name=y, type=out, value=(None), depth=4
    gate id=46: name=g1, type=not, value=(y=None), depth=1
    gate id=47: name=g2, type=not, value=(y=None), depth=1
    gate id=48: name=g3, type=and3, value=(y=None), depth=2
    gate id=49: name=g4, type=and3, value=(y=None), depth=2
    gate id=50: name=g5, type=and3, value=(y=None), depth=2
    gate id=51: name=g6, type=and3, value=(y=None), depth=1
    gate id=52: name=g7, type=or4, value=(y=None), depth=3
```

- We see that all input gates are initialized with boolean values.
- All other gates value are still `None`.

- **PyCirc** has a `step` method which triggers the logic function of every logic gate whose inputs are initialized to boolean values.

```
mux2.step()

for g in mux2.gates:
    print(g)

gate id=39: name=x0, type=inp, value=(0), depth=0
gate id=40: name=x1, type=inp, value=(1), depth=0
gate id=41: name=x2, type=inp, value=(0), depth=0
gate id=42: name=x3, type=inp, value=(1), depth=0
gate id=43: name=s1, type=inp, value=(1), depth=0
gate id=44: name=s2, type=inp, value=(0), depth=0
gate id=45: name=y, type=out, value=(None), depth=4
gate id=46: name=g1, type=not, value=(y=0), depth=1
gate id=47: name=g2, type=not, value=(y=1), depth=1
gate id=48: name=g3, type=and3, value=(y=None), depth=2
gate id=49: name=g4, type=and3, value=(y=None), depth=2
gate id=50: name=g5, type=and3, value=(y=None), depth=2
gate id=51: name=g6, type=and3, value=(y=0), depth=1
gate id=52: name=g7, type=or4, value=(y=None), depth=3
```

- We now see that also gates  $g_1$  and  $g_2$  are initialized to boolean values.
- From the diagram of MUX2 we see that  $g_1 = \neg s_1$ .
- Since  $s_1 = 1$ , we get  $g_1 = 0$ .
- From the diagram we see that  $g_2 = \neg s_2 = \neg 0 = 1$ .
- All other gates are still in None state.
- To reach the output gate, we need to apply the `step` method three more times.
- The number of times depends on the **depth** of the circuit.

```
mux2.step()

for g in mux2.gates:
    print(g)

gate id=39: name=x0, type=inp, value=(0), depth=0
gate id=40: name=x1, type=inp, value=(1), depth=0
gate id=41: name=x2, type=inp, value=(0), depth=0
gate id=42: name=x3, type=inp, value=(1), depth=0
gate id=43: name=s1, type=inp, value=(1), depth=0
gate id=44: name=s2, type=inp, value=(0), depth=0
gate id=45: name=y, type=out, value=(None), depth=4
gate id=46: name=g1, type=not, value=(y=0), depth=1
gate id=47: name=g2, type=not, value=(y=1), depth=1
gate id=48: name=g3, type=and3, value=(y=0), depth=2
gate id=49: name=g4, type=and3, value=(y=0), depth=2
gate id=50: name=g5, type=and3, value=(y=0), depth=2
```

```
gate id=51: name=g6, type=and3, value=(y=0), depth=1
gate id=52: name=g7, type=or4, value=(y=None), depth=3
```

```
mux2.step()
```

```
for g in mux2.gates:
    print(g)
```

```
gate id=39: name=x0, type=inp, value=(0), depth=0
gate id=40: name=x1, type=inp, value=(1), depth=0
gate id=41: name=x2, type=inp, value=(0), depth=0
gate id=42: name=x3, type=inp, value=(1), depth=0
gate id=43: name=s1, type=inp, value=(1), depth=0
gate id=44: name=s2, type=inp, value=(0), depth=0
gate id=45: name=y, type=out, value=(None), depth=4
gate id=46: name=g1, type=not, value=(y=0), depth=1
gate id=47: name=g2, type=not, value=(y=1), depth=1
gate id=48: name=g3, type=and3, value=(y=0), depth=2
gate id=49: name=g4, type=and3, value=(y=0), depth=2
gate id=50: name=g5, type=and3, value=(y=0), depth=2
gate id=51: name=g6, type=and3, value=(y=0), depth=1
gate id=52: name=g7, type=or4, value=(y=0), depth=3
```

```
mux2.step()
```

```
for g in mux2.gates:
    print(g)
```

```
gate id=39: name=x0, type=inp, value=(0), depth=0
gate id=40: name=x1, type=inp, value=(1), depth=0
gate id=41: name=x2, type=inp, value=(0), depth=0
gate id=42: name=x3, type=inp, value=(1), depth=0
gate id=43: name=s1, type=inp, value=(1), depth=0
gate id=44: name=s2, type=inp, value=(0), depth=0
gate id=45: name=y, type=out, value=(0), depth=4
gate id=46: name=g1, type=not, value=(y=0), depth=1
gate id=47: name=g2, type=not, value=(y=1), depth=1
gate id=48: name=g3, type=and3, value=(y=0), depth=2
gate id=49: name=g4, type=and3, value=(y=0), depth=2
gate id=50: name=g5, type=and3, value=(y=0), depth=2
gate id=51: name=g6, type=and3, value=(y=0), depth=1
gate id=52: name=g7, type=or4, value=(y=0), depth=3
```

## ▼ Getting the circuit output

- After initializing the circuit, we can run it, get the output, and print it.
- Now all gates are initialized and we can extract the circuit outcome by the **PyCirc get method**.

```
o = mux2.get()
```

```
print(o)
```

```
y=0
```

- This is of course not the normal way to use the circuit for computation.
- It is intended for exhibiting the way a logical circuit operates and for debugging.
- The straightforward way to compute the output of a circuit is quite simple

```
o = mux2(a)
print("Input:", a)
print("Output:", o)
```

```
Input: x3=1, x2=0, x1=1, x0=0, s2=0, s1=1
Output: y=0
```

- In Python it is very easy to turn an object to also serve as a function ("callable object").
- The circuit handle `mux2` serves as a function too!
- So in one line `o = mux2(a)` we perform all the following things

1. Initialize the circuit input gates with the assignment `a`.
2. Perform the `step()` method repeatedly in order to reach the output gates .
3. Return the circuit output via the `get` method.

- In some circumstances, we may have to initialize the input gates one by one.
- In such cases we can use the `run()` method for performing the computation, and the use the `get()` method for obtaining the circuit output

```
# Obtain handles to MUX2 input gates
x0 = mux2["x0"]          # mux2["x0"] is a handle to gate "x0"
x1 = mux2["x1"]
x2 = mux2["x2"]
x3 = mux2["x3"]
s1 = mux2["s1"]
s2 = mux2["s2"]
```

```
# Now we have handles to all MUX2 input gates, we can do
# all kind of things with them:
```

```
x0.set(0)
x1.set(0)
x2.set(1)
x3.set(1)
```

```
s1.set(1)
s2.set(0)

mux2.run()                                # Running the circuit

o = mux2.get()                            # Obtaining the output
print("The output is:")
print(o)

The output is:
y=0
```

- A shorter way to do the same thing is:

```
mux2["x0"].set(0)                      # mux2["x0"] is a handle to gate "x0"
mux2["x1"].set(0)
mux2["x2"].set(1)
mux2["x3"].set(1)
mux2["s1"].set(1)
mux2["s2"].set(0)

mux2.run()                                # Running the circuit

o = mux2.get()                            # Obtaining the output
print("The output is:")
print(o)

The output is:
y=0
```

- The output is also a Python dictionary which maps the circuit output names to their respective values.
- In our example, the circuit has only one output 'y'.
- Thus, we get a one key assignment  $y=0$ .
- The circuit object can also be used as a function for performing the circuit action.
- So instead of running three different commands

```
mux2.set(a)
mux2.run()
o = mux2.get()
```

We only need one command

```
o = mux2(a)
```

- However, in some cases we need to go step by step, so we need to go a little bit slower.
- For example, in order to observe intermediate values of the logic gates, we may need to initialize the circuit with the set method and proceed to the output step by step.

## ▼ Assignment Iterator

- The **Assign.iterator** iterator is very useful for producing all possible outcomes of a given circuit.
- Here is a code for producing all the outcomes of the circuit **HAM**

```
Input = [x.name for x in ham.input]           # we need the names of the inputs
Output = [y.name for y in ham.output]          # we also want to print the output names
print("Input:", Input)
print("Output:", Output)

for a in Assign.iterator(Input):
    o = ham(a)
    print("ham: %s => %s" % (a.bits(), o.bits()))

Input: ['x1', 'x2', 'x3', 'x4']
Output: ['y1', 'y2', 'y3']
ham: 0000 => 000
ham: 0001 => 101
ham: 0010 => 000
ham: 0011 => 100
ham: 0100 => 111
ham: 0101 => 010
ham: 0110 => 111
ham: 0111 => 011
ham: 1000 => 000
ham: 1001 => 101
ham: 1010 => 000
ham: 1011 => 000
ham: 1100 => 111
ham: 1101 => 010
ham: 1110 => 011
ham: 1111 => 111
```

- Here is a code snippet for generating the truth table for the cell **HAM**.

```
Input = [x.name for x in ham.input]
Output = [y.name for y in ham.output]
names = Input + Output
head = " ".join(names)
```

```

print(head)

for a in Assign.iter(Input):
    o = ham(a)
    bits = tuple(a() + o())
    line = len(bits) * "%d " % bits
    print(line)

```

```

x1 x2 x3 x4 y1 y2 y3
0 0 0 0 0 0 0
0 0 0 1 1 0 1
0 0 1 0 0 0 0
0 0 1 1 1 0 0
0 1 0 0 1 1 1
0 1 0 1 0 1 0
0 1 1 0 1 1 1
0 1 1 1 0 1 1
1 0 0 0 0 0 0
1 0 0 1 1 0 1
1 0 1 0 0 0 0
1 0 1 1 0 0 0
1 1 0 0 1 1 1
1 1 0 1 0 1 0
1 1 1 0 0 1 1
1 1 1 1 1 1 1

```

- Two circuits are called **equivalent** if they have the same boolean function.
- Here is a **PyCirc** code for implementing an algorithm that checks if two circuits are equivalent.

```
# Check if two logic circuities are equivalent
# that is: have identical truth tables.
```

```

def is_equiv(circ1, circ2):
    Inp1 = [g.name for g in circ1.input]
    Inp2 = [g.name for g in circ2.input]
    if not len(Inp1) == len(Inp2):
        return False
    for a in Assign.iter(Inp1):
        bits1 = circ1(a).bits()
        bits2 = circ2(a).bits()
        if not bits1 == bits2:
            print("a=%s, out1=%s, out2=%s" % (a, bits1, bits2))
            return False

    return True

```

- In our cell library we have two definitions of the **cell MUX2**

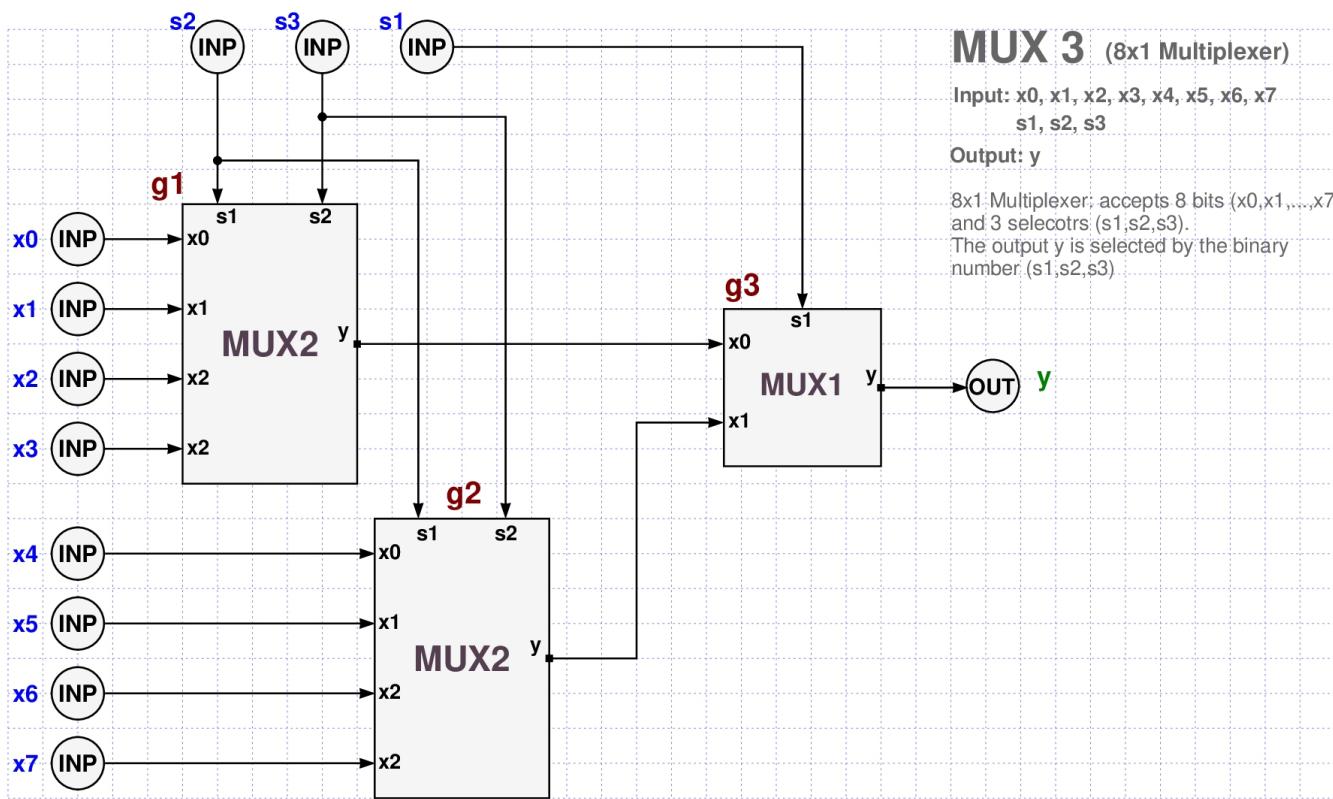
- A long definition: "[mux2.py](#)"
  - A compressed definition: "[mux2b.py](#)"
- Having two definitions for the same **cell** is not a good idea, but in some circumstances is required for testing and research.
  - In such cases it is a must that we have a tool for checking that indeed these definitions are equivalent! Or else we're in deep trouble ...
  - This is where we use our **is\_equiv** utility:

```
load("mux2")
load("mux2b")
mux2 = PyCirc["mux2"]
mux2b = PyCirc["mux2b"]
print("Checking equivalence:")
is_equiv(mux2, mux2b)

path = ['c:/eda/pycirc/lib', 'd:/cmfl/code/logcirc/lib1', 'https://samyzaf.com/pycirc/lib/mux2.py
Cell = mux2: Validity check: OK.
Loaded circuit mux2 from: https://samyzaf.com/pycirc/lib/mux2.py
path = ['c:/eda/pycirc/lib', 'd:/cmfl/code/logcirc/lib1', 'https://samyzaf.com/pycirc/lib/mux2b.py
Cell = mux2b: Validity check: OK.
Loaded circuit mux2b from: https://samyzaf.com/pycirc/lib/mux2b.py
Checking equivalence:
True
```

## ▼ 8x1 Multiplexer Design

- Now we build an 8x1 Multiplexer circuit (aka **MUX3**) by using our **MUX2** circuit as one of its building blocks (two instances of MUX2 are needed).
- We also need one instance of 2x1 Multiplexer (aka **MUX1**), which we leave to the student as an easy exercise.



- As you can see from the diagram we now have 8 inputs bits:  $x_0, x_1, x_2, x_3, x_4, x_5, x_6, x_7$ , and one output bit:  $y$ .
- We only need 3 logic gates:  $g_1, g_2$ , and  $g_3$ .
  - $g_1$  and  $g_2$  are two instances of MUX2,
  - $g_3$  is an instance of MUX1.
- Here is the code for creating a PyCirc MUX3 object.
  - Notice that this time we are using compressed notation technique for creating the 11 input gates in one line!
  - The compressed notation can be used everywhere in PyCirc and saves a lot of typing!
  - Note that this is the python code. Within a circuit file you must remove the opening Define and closing EndDef commands!

```
need("mux2")
```

```
Define("mux3")
GATE("x<0:7>; s<1:3>", type="inp")
GATE("y", type="out")
```

```
GATE("g1", type="mux2")
GATE("g2", type="mux2")
GATE("g3", type="mux1")
```

```
WTRF("x0" "s1/x0")
```

```

    WIRE("x1", "g1/x1")
    WIRE("x2", "g1/x2")
    WIRE("x3", "g1/x3")
    WIRE("x4", "g2/x0")
    WIRE("x5", "g2/x1")
    WIRE("x6", "g2/x2")
    WIRE("x7", "g2/x3")
    WIRE("s2", "g1/s1")
    WIRE("s2", "g2/s1")
    WIRE("s3", "g1/s2")
    WIRE("s3", "g2/s2")
    WIRE("s1", "g3/s1")
    WIRE("g1/y", "g3/x0")
    WIRE("g2/y", "g3/x1")
    WIRE("g3/y", "y")
EndDef()

```

```

Cell = mux3: Validity check: OK.
<pycirc.pycirc.PyCirc at 0x7f011d409290>

```

```

mux3 = PyCirc["mux3"]

for g in mux3.gates:
    print(g)

    gate id=81: name=x0, type=inp, value=(None), depth=0
    gate id=82: name=x1, type=inp, value=(None), depth=0
    gate id=83: name=x2, type=inp, value=(None), depth=0
    gate id=84: name=x3, type=inp, value=(None), depth=0
    gate id=85: name=x4, type=inp, value=(None), depth=0
    gate id=86: name=x5, type=inp, value=(None), depth=0
    gate id=87: name=x6, type=inp, value=(None), depth=0
    gate id=88: name=x7, type=inp, value=(None), depth=0
    gate id=89: name=s1, type=inp, value=(None), depth=0
    gate id=90: name=s2, type=inp, value=(None), depth=0
    gate id=91: name=s3, type=inp, value=(None), depth=0
    gate id=92: name=y, type=out, value=(None), depth=3
    gate id=93: name=g1, type=mux2, value=(y=None), depth=1
    gate id=94: name=g2, type=mux2, value=(y=None), depth=1
    gate id=95: name=g3, type=mux1, value=(y=None), depth=2

```

```

mux3 = PyCirc["mux3"]

for g in mux3.gates:
    print("%s = %s" % (g.name, g.get()))

x0 = None

```

```
x1 = None
x2 = None
x3 = None
x4 = None
x5 = None
x6 = None
x7 = None
s1 = None
s2 = None
s3 = None
y = None
g1 = y=None
g2 = y=None
g3 = y=None

for w in mux3.wires:
    print(w)

        target=gate id=94: name=g2, type=mux2, value=(y=None), depth=1
        source=None
        target=x0
    wire id=107:
        source=gate id=86: name=x5, type=inp, value=(None), depth=0
        target=gate id=94: name=g2, type=mux2, value=(y=None), depth=1
        source=None
        target=x1
    wire id=108:
        source=gate id=87: name=x6, type=inp, value=(None), depth=0
        target=gate id=94: name=g2, type=mux2, value=(y=None), depth=1
        source=None
        target=x2
    wire id=109:
        source=gate id=88: name=x7, type=inp, value=(None), depth=0
        target=gate id=94: name=g2, type=mux2, value=(y=None), depth=1
        source=None
        target=x3
    wire id=110:
        source=gate id=90: name=s2, type=inp, value=(None), depth=0
        target=gate id=93: name=g1, type=mux2, value=(y=None), depth=1
        source=None
        target=s1
    wire id=111:
        source=gate id=90: name=s2, type=inp, value=(None), depth=0
        target=gate id=94: name=g2, type=mux2, value=(y=None), depth=1
        source=None
        target=s1
    wire id=112:
        source=gate id=91: name=s3, type=inp, value=(None), depth=0
        target=gate id=93: name=g1, type=mux2, value=(y=None), depth=1
        source=None
        target=s2
    wire id=113:
        source=gate id=91: name=s3, type=inp, value=(None), depth=0
        target=gate id=94: name=g2, type=mux2, value=(y=None), depth=1
        source=None
        target=s2
```

```

    ↵  ↵  ↵  ↵
wire id=114:
    source=gate id=89: name=s1, type=inp, value=(None), depth=0
    target=gate id=95: name=g3, type=mux1, value=(y=None), depth=2
    source=None
    target=s1
wire id=115:
    source=gate id=93: name=g1, type=mux2, value=(y=None), depth=1
    target=gate id=95: name=g3, type=mux1, value=(y=None), depth=2
    source=y
    target=x0
wire id=116:
    source=gate id=94: name=g2, type=mux2, value=(y=None), depth=1
    target=gate id=95: name=g3, type=mux1, value=(y=None), depth=2
    source=y
    target=x1
wire id=117:
    source=gate id=95: name=g3, type=mux1, value=(y=None), depth=2
    target=gate id=92: name=y, type=out, value=(None), depth=3
    source=y
    target=None

```

- This is quite verbose and not too helpful except for debugging.
- We can extract a more focused output with code like this.

```
for w in mux3.wires:
    print("%s => %s" % (w.source, w.target))
```

```

x0 => g1/x0
x1 => g1/x1
x2 => g1/x2
x3 => g1/x3
x4 => g2/x0
x5 => g2/x1
x6 => g2/x2
x7 => g2/x3
s2 => g1/s1
s2 => g2/s1
s3 => g1/s2
s3 => g2/s2
s1 => g3/s1
g1/y => g3/x0
g2/y => g3/x1
g3/y => y

```

```
a = Assign("x<0:7> ; s<1:3>", "00001000" + "000")
mux3.set(a)
for x in mux3.input:
    print("%s = %d" % (x.name, x.value))

g3 = mux3["g3"]
```

```

for g in mux3.in_gates(g3):
    print(g)
print("Depth =", mux3.depth)

x0 = 0
x1 = 0
x2 = 0
x3 = 0
x4 = 1
x5 = 0
x6 = 0
x7 = 0
s1 = 0
s2 = 0
s3 = 0
gate id=89: name=s1, type=inp, value=(0), depth=0
gate id=93: name=g1, type=mux2, value=(y=None), depth=1
gate id=94: name=g2, type=mux2, value=(y=None), depth=1
Depth = 3

```

```

a = Assign("x<0:7> ; s<1:3>", "00000011" + "111")
print("Input:")
print(a)
o = mux3(a)
print("Output:")
print(o)

```

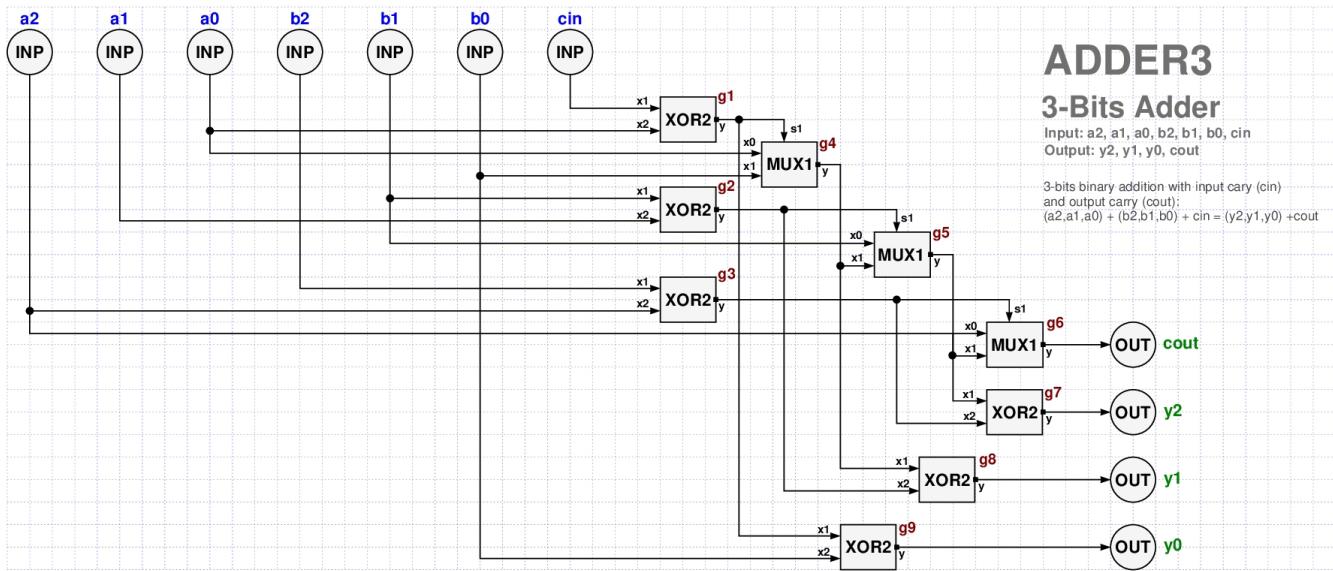
```

Input:
x0=0, x1=0, x2=0, x3=0, x4=0, x5=0, x6=1, x7=1, s1=1, s2=1, s3=1
Output:
y=1

```

## ▼ 3-bits Adder Design

- Here is a simple design for 3 bits adder with carry in (cin) and carry out (cout) bits



- This circuit accepts three types of input
  - two binary numbers:  $(a_2, a_1, a_0), (b_2, b_1, b_0)$
  - a carry in bit: `cin`.
- Its output  $(y_2, y_1, y_0)$  is the binary sum of the two numbers (with the carry added).
- In case of addition overflow, we need a carry out (`cout`) output bit as well.
- The following **PyCirc** code is the **PyCirc** model for the **ADDER3** cell.

```
# ADDER3
# Input: a2, a1, a0, b2, b1, b0, cin
# Output: y2, y1, y0, cout
```

```
Define("adder3")
GATE("a2", type="inp")
GATE("a1", type="inp")
GATE("a0", type="inp")

GATE("b2", type="inp")
GATE("b1", type="inp")
GATE("b0", type="inp")

GATE("cin", type="inp")

GATE("y2", type="out")
GATE("y1", type="out")
GATE("y0", type="out")

GATE("cout", type="out")

GATE("g1", type="xor2")
```

```

GATE("g2", type="xor2")
GATE("g3", type="xor2")
GATE("g4", type="mux1")
GATE("g5", type="mux1")
GATE("g6", type="mux1")
GATE("g7", type="xor2")
GATE("g8", type="xor2")
GATE("g9", type="xor2")

WIRE("a2", "g3/x2")
WIRE("a2", "g6/x0")
WIRE("a1", "g2/x2")
WIRE("a0", "g1/x2")
WIRE("a0", "g4/x0")
WIRE("b2", "g3/x1")
WIRE("b1", "g2/x1")
WIRE("b1", "g5/x0")
WIRE("b0", "g4/x1")
WIRE("b0", "g9/x2")
WIRE("cin", "g1/x1")
WIRE("g1/y", "g4/s1")
WIRE("g1/y", "g9/x1")
WIRE("g2/y", "g5/s1")
WIRE("g2/y", "g8/x2")
WIRE("g3/y", "g6/s1")
WIRE("g3/y", "g7/x2")
WIRE("g4/y", "g5/x1")
WIRE("g4/y", "g8/x1")
WIRE("g5/y", "g6/x1")
WIRE("g5/y", "g7/x1")
WIRE("g6/y", "cout")
WIRE("g7/y", "y2")
WIRE("g8/y", "y1")
WIRE("g9/y", "y0")
EndDef()

```

**Cell** = adder3: Validity check: OK.  
`pycirc.pycirc.PyCirc at 0x7f011d8faa90`

- This is the compressed version of this code.
- The number of lines was reduced by half! (from 46 to 23).

```

# ADDER3, compressed version
# Input: a2, a1, a0, b2, b1, b0, cin
# Output: y2, y1, y0, cout

```

```

Define("adder3")
GATE("a<2:0>", type="inp")
GATE("b<2:0>", type="inp")
GATE("cin", type="inp")
GATE("y<2:0>", type="out")
GATE("cout", type="out")

GATE("g<1:3,7:9>", type="xor2")
GATE("g<4:6>", type="mux1")

WIRE("a2", "g3/x2; g6/x0")
WIRE("a1", "g2/x2")
WIRE("a0", "g1/x2; g4/x0")
WIRE("b2", "g3/x1")
WIRE("b1", "g2/x1; g5/x0")
WIRE("b0", "g4/x1; g9/x2")
WIRE("cin", "g1/x1")
WIRE("g1/y", "g4/s1; g9/x1")
WIRE("g2/y", "g5/s1; g8/x2")
WIRE("g3/y", "g6/s1; g7/x2")
WIRE("g4/y", "g5/x1; g8/x1")
WIRE("g5/y", "g6/x1; g7/x1")
WIRE("g6/y", "cout")
WIRE("g<7:9>/y", "y<2:0>")
EndDef()

```

```

Cell = adder3: Validity check: OK.
<pycirc.pycirc.PyCirc at 0x7f011d423c90>

```

```
adder3 = PyCirc["adder3"]
```

- Lets test our adder by verifying that

$011 + 011 = 110$

```

bits = "011" + "011" + "0"
a = Assign("a<2:0>; b<2:0>; cin", bits)
o = adder3(a)
cin = a["cin"]
cout = o["cout"]
A = a.bits("a<2:0>")
B = a.bits("b<2:0>")

```

```

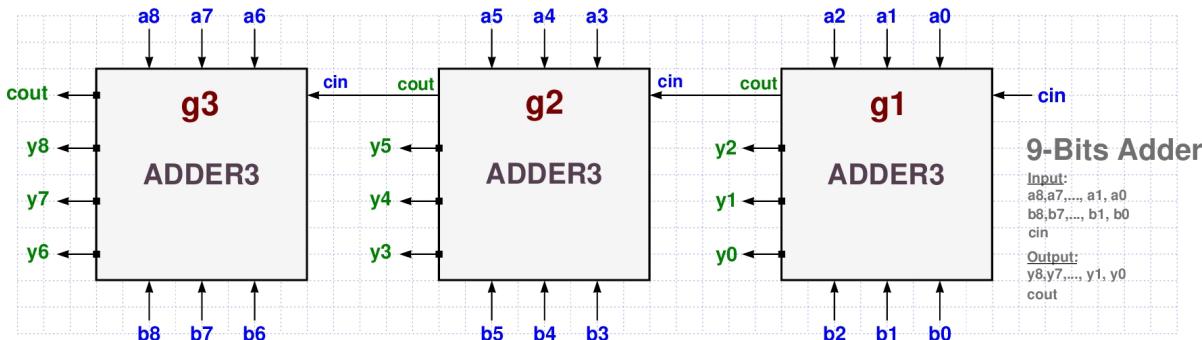
Y = o.bits("y<2:0>")
print("%s + %s = %s : cin=%s cout=%s" % (A,B,Y,cin,cout))

011 + 011 = 110 : cin=0 cout=0

```

## ▼ ADDER9 - 9-bits Adder Design

- Here is a simple **PyCirc Design Diagram** for the standard 9-bits adder with a carry in (cin) and carry out (cout) bits.
- It uses 3 gates g1, g2, g3, of type **ADDER3** which are chained by their cout/cin pins.
- **Input:**  $a<8:0> + b<8:0> + \text{cin}$
- **Output:**  $y<8:0> + \text{cout}$



- Here is a compressed **PyCirc** code for **ADDER9**:

```

# ADDER9
# Input: a8, a7, a6, a5, a4, a3, a2, a1, a0, b8, b7, b6, b5, b4, b3, b2, b1, b0,
# Output: y8, y7, y6, y5, y4, y3, y2, y1, y0, cout

need("adder3")

Define("adder9")
GATE("a<8:0>;b<8:0>", type="inp")
GATE("cin", type="inp")
GATE("y<8:0>", type="out")
GATE("cout", type="out")
GATE("g1", type="adder3")           # First ADDER3 gate
GATE("g2", type="adder3")           # Second ADDER3 gate
GATE("g3", type="adder3")           # Third ADDER3 gate

WIRE("a<0:2>", "g1/a<0:2>"),
WIRE("a<3:5>", "g2/a<0:2>"),
WIRE("a<6:8>", "g3/a<0:2>"),

```

```

WIRE("b<0:2>", "g1/b<0:2>"),
WIRE("b<3:5>", "g2/b<0:2>"),
WIRE("b<6:8>", "g3/b<0:2>"),
WIRE("cin", "g1/cin"),
WIRE("g1/cout", "g2/cin"),
WIRE("g2/cout", "g3/cin"),
WIRE("g3/cout", "cout"),
WIRE("g1/y<0:2>", "y<0:2>"),
WIRE("g2/y<0:2>", "y<3:5>"),
WIRE("g3/y<0:2>", "y<6:8>"),
EndDef()

```

**Cell** = adder9: Validity check: OK.  
 <pycirc.pycirc.PyCirc at 0x7f011d8e7e10>

- The `full_run` utility can be used for traversing all input/output pairs.
- Interactively.
- To stop: press "q".

```
adder9 = PyCirc["adder9"]
```

```
full_run(adder9)
```

```

Input:
a8=0, a7=0, a6=0, a5=0, a4=0, a3=0, a2=0, a1=0, a0=0, b8=0, b7=0, b6=0, b5=0, b4=0, b3=0
Output:
y8=0, y7=0, y6=0, y5=0, y4=0, y3=0, y2=0, y1=0, y0=0, cout=0
Press <Enter> to continue or 'q' to quit
Next?
Input:
a8=0, a7=0, a6=0, a5=0, a4=0, a3=0, a2=0, a1=0, a0=0, b8=0, b7=0, b6=0, b5=0, b4=0, b3=0
Output:
y8=0, y7=0, y6=0, y5=0, y4=0, y3=0, y2=0, y1=0, y0=1, cout=0
Press <Enter> to continue or 'q' to quit
Next?
Input:
a8=0, a7=0, a6=0, a5=0, a4=0, a3=0, a2=0, a1=0, a0=0, b8=0, b7=0, b6=0, b5=0, b4=0, b3=0
Output:
y8=0, y7=0, y6=0, y5=0, y4=0, y3=0, y2=0, y1=0, y0=1, cout=0
Press <Enter> to continue or 'q' to quit
Next? q

```

- However this is not readable and takes forever!
- Number of inputs is 17 bits, so the loop has  $2^{17} = 131072$  cycles!
- We will better off running only random assignments, and verify them manually.
- The `pycirc` package has the following utility for creating a random assignment.

```
def random_assignment(names):
    names = expand(names)
    a = Assign(names)
    for x in names:
        a[x] = randint(0,1)
    return a
```

- Here are 5 random samples on our **ADDER3** input

```
names = "a<8:0>; b<8:0>; cin"
for i in range(5):
    a = random_assignment(names)
    A = a.bits("a<8:0>")
    B = a.bits("b<8:0>")
    print(A, B, a["cin"])

00000001 000110011 0
000110000 010110001 1
111011011 100000010 0
111000011 001100110 1
011111111 111000001 1
```

- Now we can generate random inputs for **ADDER9**, get the output, and verify its correctness.

```
names = "a<8:0>; b<8:0>; cin"
while True:
    a = random_assignment(names)
    A = a.bits("a<8:0>")
    B = a.bits("b<8:0>")
    cin = a["cin"]
    print(80*"-")
    print("Input: %s + %s + %s" % (A, B, cin))
    o = adder9(a)
    Y = o.bits("y<8:0>")
    cout = o["cout"]
    print("Output: %s + %s" % (Y, cout))
    print("Verify sum: %s" % (bin(int(A,2) + int(B,2)),))
    inpstr = input("Press <Enter> to continue or q to stop: ")
    if "q" == inpstr:
        break
```

---

```
Input: 111001010 + 000010011 + 1
Output: 111011110 + 0
```

```

Verify sum: 0b111011101
Press <Enter> to continue or q to stop:
-----
Input: 110110111 + 011010010 + 1
Output: 010001010 + 1
Verify sum: 0b1010001001
Press <Enter> to continue or q to stop:
-----
Input: 000101011 + 000111000 + 0
Output: 001100011 + 0
Verify sum: 0b1100011
Press <Enter> to continue or q to stop: q

```

## ▼ Full Adder

- A full adder is a the same thing except that it does not have carry bits.
- It simply adds its two input bits and outputs the sum.
- In general, an **n-bits full adder** has  $2n$  inputs bits " $a<0:n-1>$ " + " $b<0:n-1>$ " and  $n + 1$  output bits " $y<0:n>$ ".
- We will use our **ADDER3** cell to build a full **2-bits adder**
  - by injecting a zero constant to its **cin** input,
  - and discarding its **cout** output bit.
- We will also use this opportunity to present a different style for creating a PyCirc cell.

```

# CELL: FULL ADDER 2

# We need adder3
need("adder3")

# Here we present a different style for defining a logic circuit

gates = (
    GATE("a1", type="inp")
+ GATE("a0", type="inp")
+ GATE("b1", type="inp")
+ GATE("b0", type="inp")
+ GATE("ad3", type="adder3")
+ GATE("y2", type="out")
+ GATE("y1", type="out")
+ GATE("y0", type="out")
+ GATE("g0", type="zero")
)

wires = [

```

```

Wire("a0", "ad3/a0"),
Wire("a1", "ad3/a1"),
Wire("b0", "ad3/b0"),
Wire("b1", "ad3/b1"),
Wire("g0", "ad3/a2"),
Wire("g0", "ad3/b2"),
Wire("g0", "ad3/cin"),
Wire("ad3/y0", "y0"),
Wire("ad3/y1", "y1"),
Wire("ad3/y2", "y2"),
]
fa2 = PyCirc("full_adder2", gates, wires)
pycircLib.add_circ(fa2)

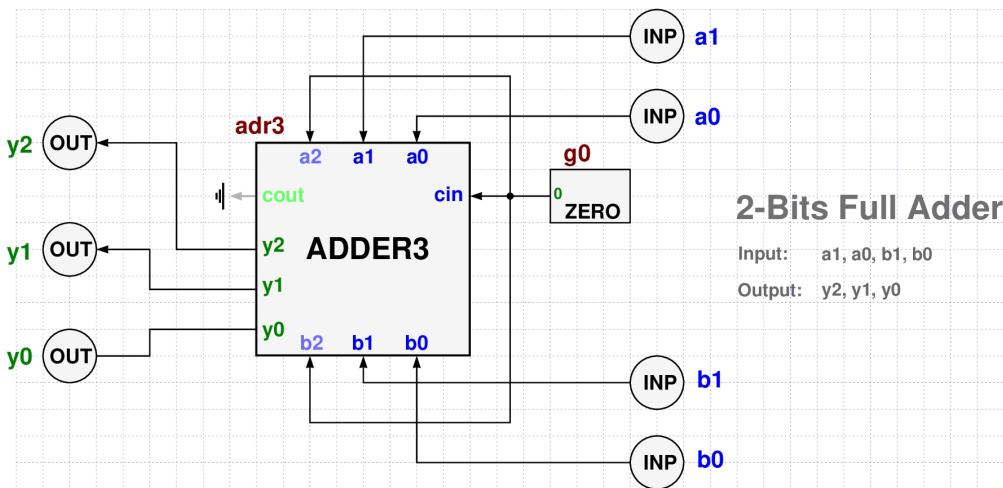
```

ATTENTION: some outputs are dangling! ad3 (adder3) : {'cout'}

Cell = full\_adder2: Validity check: OK.

<pycirc.pycirc.Cell at 0x7f011d39ed10>

- Notice that in this case, we do not have a **Define()**, **EndDef()** calls!
- We simply define a list of gates and a list of wires, and later use the class **PyCirc** to create the cell.
- The wires are created by the low level `Wire` class instead of the higher level `WIRE` function.
  - The `Wire` class is suited for generating a single wire object while `WIRE` generates multiple wires and supports compressed names.
- An output pin which is not connected to any other pin is called a **dangling pin**.
- Notice that our 2-bits full adder **FA2** has a dangling pin.
- The carry out bit (**cout**) of the gate **ad3** is dangling.
- Also notice the **constant gate** **g0** which fixes the carry in (**cin**) to a constant 0 value.
- A "dangling output" alert means that an output is not connected to anything.
  - This is OK if you intended it as we did in this example.
  - To achieve a full adder we had to discard the `cout` pin of ADDER3.



## ▼ Boolean Operators

- The **PyCirc** package contains a **logops** module which defines a small set of boolean functions.
- These functions are also called **boolean operators** since
  - they act on a variable number of boolean values.
  - return a boolean value.
- These operators are needed for designing **black box cells** that play an important role in the **VLSI** design process.
- Here are a few examples of operators we have in the **pycirc** package:
  - AND, OR, NOR, XOR, NOT, MUX.**
  - They all accept an **Assign** object as an argument,
  - and return an **Assign** object.

```
def AND(a, output="y"):
    o = Assign(output)
    for x in a:
        if a[x] == 0:
            for y in o: o[y] = 0
        return o
    for y in o: o[y] = 1
    return o
```

```
def OR(a, output="y"):
    o = Assign(output)
    for x in a:
        if a[x] == 1:
            for y in o: o[y] = 1
```

```

        return o
    for y in o: o[y] = 0
    return o

def NOR(a, output="y"):
    o = Assign(output)
    o1 = OR(a, Assign("y"))
    b = Assign("x", o1["y"])
    return NOT(b, o)

def XOR(a, output="y"):
    o = Assign(output)
    if sum(a[x] for x in a) == 1:
        for y in o: o[y] = 1
    else:
        for y in o: o[y] = 0
    return o

```

- Users can easily add more operators in client code.
- Here are two examples that we used in the development of **pycirc** for testing the various **1-bit counter cells** and the **magnitude comparator cells**.
- The first operator is simply a Python code for counting how many 1-bits a given assignment object `a` has?

```

# Count the number of 1-bits in the assignment a
def COUNT_ONES(a):
    s = sum(a())
    k = len(a).bit_length()
    bits = bin(s)[2:].zfill(k)
    names = "y<%d:1>" % (k,)
    bits = [int(y) for y in bits]
    o = Assign(names, bits)
    return o

# Magnitude Comparator Operator
# input: "a<0:n>;b<0:n>"
# output: "y<1:3>"
# If a<b returns 100
# If a==b returns 010
# If a>b returns 001
def COMPARE(a):

```

```

A = []
B = []
for name in a:
    if name[0] == "a":
        A.append(name)
    else:
        B.append(name)
A = int(a.bits(A), 2)
B = int(a.bits(B), 2)
o = Assign("y<1:3>")
if A < B:
    o.assign("100")
elif A == B:
    o.assign("010")
else:
    o.assign("001")
return o

```

```

a = Assign("x<1:5>", "01011")
o = COUNT_ONES(a)
print(o)

```

y3=0, y2=1, y1=1

- Note that the result is in numerical binary form: 011.
- The input "01011" has 3 occurrences of the bit 1, which in numerical binary form is 11.

```

a = Assign("x<1:8>", "11101011")
print("Input:", a.bits())
o = COUNT_ONES(a)
print("Output (binary):", o.bits())
print("Output (decimal):", int(o.bits(), 2))

```

```

Input: 11101011
Output (binary): 0110
Output (decimal): 6

```

- Here, the input "11101011" contains 6 bits of 1.
- As expected, the output is 110 which is a numerical binary representation of decimal 6.
- The following operators do not accept any input but produces a **constant** output.
- These are the **constant operators**.
- The **ZERO** operator produces 0.

- The **ONE** operator produces 1.
- Here are the definitions of the **ZERO** and **ONE** operators

```
def ZERO(a=None, output="y"):
    o = Assign(output)
    for y in o: o[y] = 0
    return o
```

```
def ONE(a=None, output="y"):
    o = Assign(output)
    for y in o: o[y] = 1
    return o
```

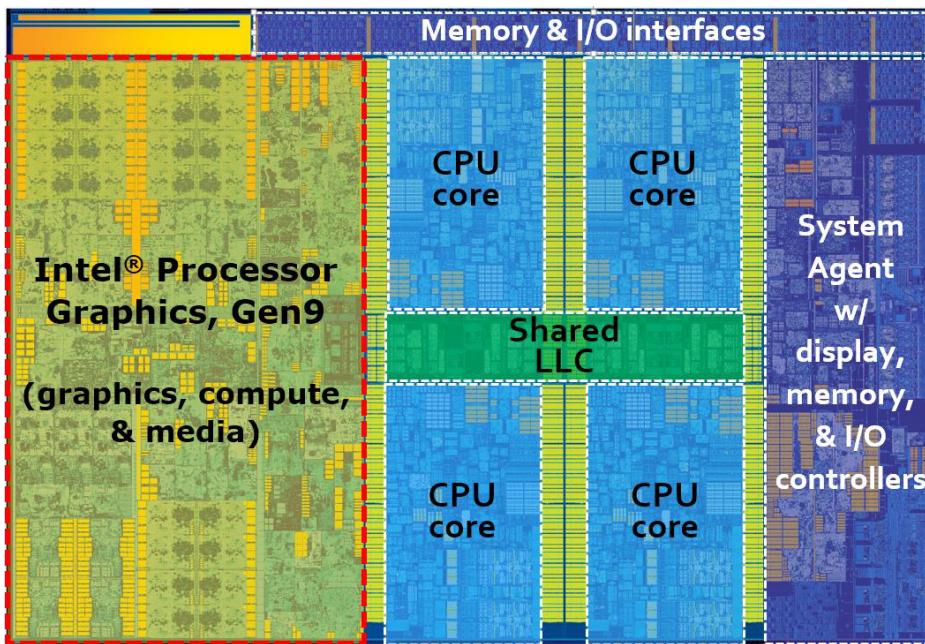
- The **Magnitude Comparator** operator acts on even length assignments only.
- It splits the input to two equal length binary numbers and compares their magnitude.

```
a = Assign("a<0:7>; b<0:7>", "00101101" + "00110101")
o = COMPARE(a)
print(o)
```

y1=1, y2=0, y3=0

## ▼ Creating Cells with the Cell Class

- VLSI design usually means designing very large logic circuits consisting of millions and even billions of elements.
- This is achieved by dividing the main circuit to a dozen or so sub-circuits, usually called **sections**.
- Each **section** is divided to a set of smaller cells, usually called **blocks**.
- Each **block** is partitioned to smaller cells, usually called **functional unit blocks** (or **fubs** for short).
- And finally, each functional unit is partitioned to smaller cells taken from established **cell libraries**.
- This design method is usually called **Hierarchical Design**.
- For example, here is a high level hierarchical view of Intel's **Skylake** cpu

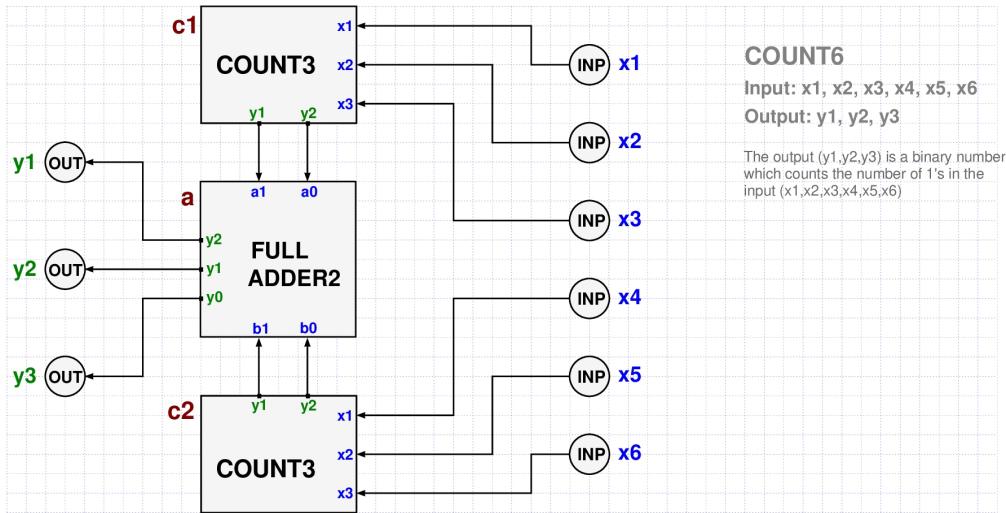


- It consists of roughly 5 billion transistors and 20 billion wires.
- In the early design phase, only a small number of the **cell** designs are available.
- Many other **cells** are replaced by "black boxes" that simulate **cells**, but their full circuit design is postponed to a later stage after passing many fire tests that verify the feasibility of the overall design.
- These simulation tests determine many of the desired properties and parameters for these **cells**, and thus provide a lot of information and clues needed to design them efficiently.
- In such scenarios, a **Logic Cell** is viewed as a "black box" with entry and exit points that can be defined more conveniently by means of simple numerical software algorithms.
- **PyCirc** provides a high level **Cell** class for defining such **cells**.
- So we have two ways to define a new **cell**:
  1. By defining a **PyCirc** circuit as in the examples above
  2. By defining a **boolean operator** numerically.
    - A **cell** defined by an operator is named **black box** or **box** for short.
    - It is a place holder for a real circuit which is not yet available, but the overall design need to be tested before it is decided if its design is feasible.
- Here is an example of a 4x3 **cell** that is defined by the **Cell** class.

```
count3 = Cell("count3", operator=COUNT_ONES, input="x<1:3>", output="y<1:2>", depth=1)
# currently all box type Cells are stored in the default PyCirc library called pycircLib
pycircLib.add(count3)
```

- It accepts a 4-bits assignment and outputs a 3-bits assignment.

- It counts the number of 1-bits in the input.
- The operator **COUNT\_ONES** was defined in the section above.
- We can now use **count3** as a cell type and use it to define more complex cells.
- As an example, let's define a **COUNT6** circuit by using two gates of type **COUNT3**.



- The plan is straightforward:
  - **COUNT6** accepts 6 input bits:  $x_1, x_2, x_3, x_4, x_5, x_6$ .
  - The first 3 bits  $x_1, x_2, x_3$ , are assigned to the gate **c1** whose type is **COUNT3**.
  - The last 3 bits  $x_4, x_5, x_6$ , are assigned to the gate **c2** whose type is also **COUNT3**.
  - The outputs of **c1** and **c2** are sent to gate **a** which is a **FULL\_ADDER2**.
  - The gate **a** is adding up the two numbers and sends its output to  $y_1, y_2, y_3$ .
- Here is the **PyCirc Program** for the **COUNT6** circuit.

```
Define("count6")
GATE("x<1:6>", type="inp")
GATE("y<1:3>", type="out")
GATE("c1", type="count3")           # Gate "c1" of type count3
GATE("c2", type="count3")           # Gate "c2" of type count3
GATE("a", type="full_adder2")

WIRE("x<1:3>", "c1/x<1:3>")
WIRE("x<4:6>", "c2/x<1:3>")
WIRE("c1/y1", "a/a1")
WIRE("c1/y2", "a/a0")
WIRE("c2/y1", "a/b1")
WIRE("c2/y2", "a/b0")
WIRE("a/y<2:0>", "y<1:3>")
EndDef()
```

```
Cell = count6: Validity check: OK.
<pycirc.pycirc.PyCirc at 0x7f011d396b50>
```

- Here is the Python code for adding some of the box **cells** in **PyCirc**.
- See the **factory** module in the **PyCirc** package for more examples.

```
pycircLib.add_box(name="and2", operator=AND, input="x<1:2>", output=["y"])
pycircLib.add_box(name="and3", operator=AND, input="x<1:3>", output=["y"])
pycircLib.add_box(name="and4", operator=AND, input="x<1:4>", output=["y"])
pycircLib.add_box(name="and5", operator=AND, input="x<1:5>", output=["y"])
pycircLib.add_box(name="and6", operator=AND, input="x<1:6>", output=["y"])
pycircLib.add_box(name="and7", operator=AND, input="x<1:7>", output=["y"])
pycircLib.add_box(name="and8", operator=AND, input="x<1:8>", output=["y"])
```

- We can also use Python loops to add box **cells** to our cell library.
- The following Python loop, adds 32 box **cells** to the **PyCirc cell library**
  - 8 **OR** box cells: **OR2**, **OR3**, ..., **OR8**
  - 8 **XOR** box cells: **XOR2**, **XOR3**, ..., **XOR8**
  - 8 **NOR** box cells: **NOR2**, **NOR3**, ..., **NOR8**

```
for k in range(2,9):
    inp = "x<1:%s>" % (k,)
    name = "or" + str(k)
    pycircLib.add_box(name, operator=OR, input=inp, output=["y"])
    name = "xor" + str(k)
    pycircLib.add_box(name, operator=XOR, input=inp, output=["y"])
    name = "nor" + str(k)
    pycircLib.add_box(name, operator=NOR, input=inp, output=["y"])
    name = "nand" + str(k)
    pycircLib.add_box(name, operator=NAND, input=inp, output=["y"])
```

## ▼ Advanced Topics -- To be Continued ...

- For the more experienced students we present here some more advanced usage of the PyCirc package will be added within the near future. To be continued ...

```
from IPython.display import HTML
from urllib.request import urlopen
css = urlopen("https://samyzaf.com/css/pycirc.css").read().decode('utf-8')
HTML('<style>{}</style>'.format(css))
```

---

✓ 0s completed at 8:57 PM

